

# Proof

# Mark Scheme

1. (a)  $5n$  1  
*B1 cao*
- (b) (i)  $5n + 5(n \pm 1)$   
 $10n \pm 5$   
 $5(2n \pm 1)$   
Both 5 and  $2n \pm 1$  are odd 2  
*M1 for  $5n + 5(n \pm 1)$  or  $10n \pm 5$  or for  $5(2n \pm 1)$*   
*A1 for stating both 5 and  $2n \pm 1$  are odd and  $\text{odd} \times \text{odd} = \text{odd}$*   
*oe*
- (ii)  $5n \times 5(n \pm 1)$   
 $25n(n \pm 1)$   
25 is odd, one of  $n$  or  $n \pm 1$  is odd so  $\text{odd} \times \text{even} \times \text{odd} = \text{even}$  3  
*M1 for  $5n \times 5(n \pm 1)$*   
*A1 for realises that one of  $n$  and  $n \pm 1$  will be even or considers  $5n$  or  $5(n \pm 1)$  for both odd and even*  
*A1 for establishing correct result oe*  
*(SC if M0, MO awarded in part (b) B1 for using in b(i) or (ii) a numerical argument with more than 2 examples)*  
*(SC for  $5n$  and  $5n \pm 1$  used B1 in (i) and B1 in (ii) for fully reasoned argument)*

[6]

2. Printed result proved algebraically 4  
 $2n$  and  $2n + 2$ , where  $n$  is an integer  
 $(2n)^2 + (2n + 2)^2 = 4n^2 + 4n^2 + 8n + 4 = 8(n^2 + n) + 4$   
 $8(n^2 + n)$  is always a multiple of 8 so  
 $8(n^2 + n) + 4$  is never a multiple of 8. oe  
*B1 for either  $2n$  or  $2n + 2$*   
*M1 for correct expansion*  
*A1 for correct simplified algebraic expression with some factorisation*  
*A1 convincing conclusion to the mathematical argument*

[4]

3. Either  $(n^2 + 2n + 1) - (n^2 - 2n + 1) = 4n$   
 or  $(n + 1 + n - 1)(n + 1 - (n - 1)) = 2n \times 2 = 4n$  3

*B1 + B1 for  $(n^2 + 2n + 1) - (n^2 - 2n + 1)$  must have brackets for the 2<sup>nd</sup> B1*

*B1 for  $4n$*

**Or**

*B1 for either  $(n + 1 + n - 1)$  or  $(n + 1 - (n - 1))$*

*B1 for  $(n + 1 + n - 1)(n + 1 - (n - 1))$*

*B1 for  $4n$*

*SC:  $n^2 + 2n + 1 - n^2 - 2n + 1 = 4n$  is 2/3*

[3]

4. 7 which is not even 2  
 $2^2 + 3 =$

*B2*

*(B1 for correctly evaluating  $n^2 + 3$  with a prime number value for  $n$ .)*

[2]

5.  $(2m + 1)^2 = 4m^2 + 4m + 1$   
 $(2n + 1)^2 = 4n^2 + 4n + 1$   
 Sum =  $4m^2 + 4n^2 + 4m + 4n + 2$   
 $= 4(m^2 + n^2 + m + n) + 2$  3

*B1 for  $(2m + 1)^2$*

*B1 for sum of correct expansion of 2 correct expressions for different odd squares*

*B1 fully correct answer including the factor 4, and a clear remainder of 2*

*SC B1 for  $(n + 2)^2 + n^2$  oe*

[3]